

MPM 2D

FACTORING SIMPLE TRINOMIALS $x^2 + bx + c$

Consider the expanding and simplifying of each expression:

$$\textcircled{1} \quad (x + 3)(x + 4)$$

$$\begin{aligned} &= x^2 + 4x + 3x + (3)(4) \\ &= x^2 + 7x + 12 \end{aligned}$$

$$\textcircled{2} \quad (n + 6)(n - 3)$$

$$\begin{aligned} &= n^2 - 3n + 6n - 18 \\ &= n^2 + 3n - 18 \end{aligned}$$

$$\textcircled{3} \quad (y - 4)^2$$

The key to reversing the process, that is to factor the simple trinomial into its 2 binomial factors, lies with the highlighted values. In $\textcircled{1}$, the last term (the constant term; the "y-intercept") was determined by **MULTIPLYING** the last terms of each binomial. In other words, the "+12" was obtained from multiplying "+3" by "+4". The same two numbers were used to obtain the coefficient of the second term, or linear term, by **ADDING** the coefficients of the like terms.

$$\left. \begin{array}{l} \underline{3} \times \underline{4} = 12 \\ \underline{3} + \underline{4} = 7 \end{array} \right\} \quad \begin{array}{l} x^2 + 7x + 12 \\ \swarrow \quad \searrow \\ = (x + 3)(x + 4) \end{array}$$

The x^2 term is divided into 2 x 's and the factors of 12 (+3 and +4) were connected to each x -factor!

EXERCISE: Factor each of the following trinomials.

$$1. \quad x^2 + 8x + 15$$

$$2. \quad x^2 - 8x - 20$$

$$3. \quad k^2 + k - 30$$

$$4. \quad n^2 - 11n + 28$$

$$5. \quad x^2 - 12x + 36$$

$$6. \quad m^2 + 10m - 24$$

$$7. \quad -2x^3 + 42x^2 - 160x$$

$$8. \quad w^2 + 5wk - 6k^2$$

$$9. \quad 4at^2 + 32at + 64a$$

$$10. \quad -6x^2 + 78xy - 72y^2$$