

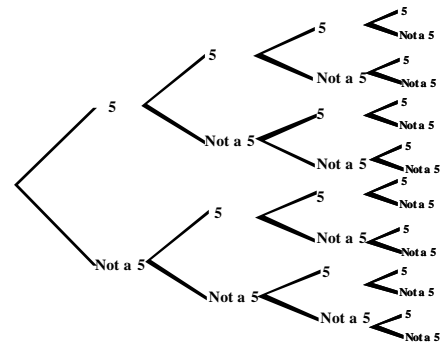
## MDM 4U

### BINOMIAL DISTRIBUTIONS

where  $X$  = random variable  
 $B$  = binomial distribution  
 $n$  = number of trials  
 $p$  = probability of success  
 $q$  = probability of failure ( $q = 1 - p$ )  
 $E(x)$  = expectation  
 $P(X=x)$  = probability of a set number of successes in  $n$  trials

1. Consider the experiment of rolling a die 4 times. The tree diagram to the right indicates the options of rolling or not rolling a 5.

Determine the probability distribution of the number of 5's that appear.



2. A die is rolled 6 times. Let  $X$  = number of 4's that appear.  
 A) What is the expected number of 4's?  
 B) Determine the probability of the expected number of 4's.
3. A die is rolled 60 times. Let  $X$  = number of 4's that appear.  
 A) What is the expected number of 4's?  
 B) Determine the probability of the expected number of 4's.
4. If the manufacturing plant of M&Ms produces 40% red candies and randomly distributes all candies into different sized bags,  
 A) what is the expected number of red candies in a bag of 10 candies?  
 B) what is the expected number of red candies in a bag of 200 candies?  
 C) what are the probabilities of these expected number of candies in a bag?  
 D) what is the probability of getting at least 2 red candies in a bag of 10 candies?
5. Given  $X \sim B(n, p)$  and the table of probabilities, determine the values of  $n$ ,  $E(x)$ , and  $p$ .

$X$	0	1	2	3	4
$P(X = x)$	$\frac{17}{125}$	$\frac{26}{125}$	$\frac{43}{125}$	$\frac{21}{125}$	$\frac{18}{125}$

ANSWERS: 2) 1; .4019, 3) 10; .1370, 4) 4; 80; .251; .058, 5) 125; 1.976; .0158