

## MCR 3U

### RATIONAL FUNCTIONS

#### STEPS TO SKETCH RATIONAL FUNCTIONS

1. State the domain and range of the function.

$$\{x \in R, x \neq \underline{\hspace{1cm}}\}$$

$$\{y \in R, y \neq \underline{\hspace{1cm}}\}$$

2. The D and R represent areas where the graph of the function does not exist. These “areas” are designated by vertical and horizontal dashed lines and are known as **ASYMPTOTES**.

Go to the location in the coordinate system where the asymptotes are located and draw horizontal and vertical dashed lines through the point.

3. The “a” value [located in the numerator of the rational function] is used to sketch points that belong to the rational function.

State at least 4 pairs of factors that multiply to the “a” value. [use decimals, if necessary]. These pairs of factors translate into ordered pairs relative to the “new origin”.

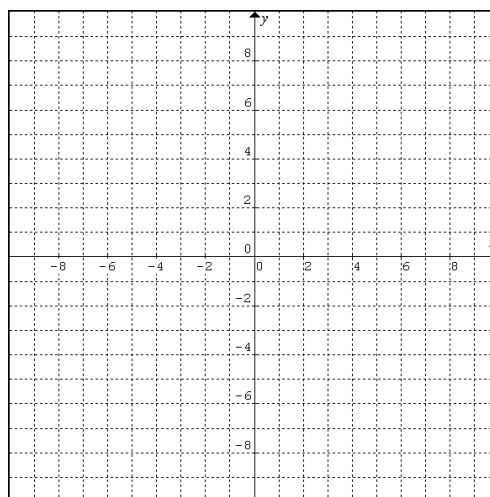
From the “new origin”, [where the asymptotes intersect], use the pairs of factors determined by the “a” value to plot points.

#### EXAMPLE:

$$f(x) = \frac{6}{x-3} - 4$$

$$\{x \in R, x \neq 3\}$$

$$\{y \in R, y \neq -4\}$$



Since  $a = 6$ , pairs of factors are:

$$1 \times 6, \quad -1 \times -6$$

$$2 \times 3, \quad -2 \times -3$$

From  $(3, -4)$  [the new origin], use  $1 \times 6$  by going 1 unit right and 6 units up, and plot a point. Then from the new origin, go 6 units right and 1 unit up, and plot a point. Do the same for the other pairs of factors.

Draw a smooth curve through the points and approaching the asymptotes, without touching the asymptotes. Draw arrows at each end of each curve.

## **EXERCISE:**

**PART A:** Sketch and state the properties of each rational function.

1.  $f(x) = \frac{6}{x} + 3$

2.  $y = \frac{4}{x-2} - 2$

3.  $f(x) = \frac{3}{x+4} + 2$

4.  $h(x) = \frac{-8}{x-1}$

5.  $k(x) = \frac{2}{x+5} - 3$

6.  $g(x) = 4 - \frac{1}{x}$

7.  $y = 3 + \frac{9}{x+1}$

8.  $a(x) = \frac{5}{x}$

9.  $t(x) = 6 - \frac{3}{x-2}$

10.  $f(x) = \frac{10}{x+2} + 2$

**PART B:** Determine the equation of each rational function.

